

$$\frac{8x^{-2} - 2x^{-1}}{10x^{-1} - 6x^{-2}}$$

$$\begin{array}{c} \frac{x^2}{1} \frac{8}{x^2} \\ - \\ \frac{2x^2}{x} \frac{1}{1} \end{array}$$

$$\begin{array}{c} \frac{x^2}{1} \frac{10}{x} \\ - \\ \frac{6x^2}{x^2} \frac{1}{1} \end{array}$$

$$\frac{8 - 2x}{10x - 4} \rightarrow \frac{2(4-x)}{2(5x-3)}$$

# 11.4 divide polynomials

$$\frac{7}{2} = 3\frac{1}{2}$$

$$\begin{array}{r} 3 \\ 2 \overline{) 7} \\ -6 \\ \hline 1 \end{array}$$

$$\frac{9x^3 + 6x^2 - 12x + 15}{3x} \quad \underline{\text{divide}}$$

$$\left( \frac{9x^3}{3x} \right) + \left( \frac{6x^2}{3x} \right) - \left( \frac{12x}{3x} \right) + \left( \frac{15}{3x} \right)$$

$$3x^2 + 2x - 4 + \frac{5}{x}$$

$$\left( \frac{18x^7}{-2x^4} - \frac{9x^6}{-2x^4} + \frac{20x^5}{-2x^4} - \frac{10x^4}{-2x^4} \right) \div (-2x^4)$$

divide

monomial

$$-9x^3 + \frac{9}{2}x^2 - 10x + 5$$

$$\begin{array}{r} x^2 - 3x - 5 \\ \hline x-2 \end{array}$$

$$\begin{array}{r} x^2 - 3x - 5 \\ \hline x-2 \end{array}$$

~~$x^2 - 3x - 5$~~   
 ~~$x-2$~~   
not useful

$$\begin{array}{r} x-1 - \frac{7}{x-2} \\ \hline x-2 \left( \begin{array}{r} x^2 - 3x - 5 \\ -x^2 + 2x \end{array} \right) \\ \hline -x - 5 \\ +x + 2 \\ \hline -7 \end{array}$$

$$\begin{array}{r} \rightarrow 2 \boxed{\frac{6}{7}} \quad \frac{153}{7} \\ 7 \boxed{153} \\ - 14 \downarrow \\ \hline 13 \end{array}$$

$$\begin{array}{r} \boxed{w} \quad \boxed{w} \quad \boxed{w} \quad \boxed{-7} \quad \boxed{w} \\ \hline \end{array}$$

$\boxed{w}$

check  $(x-1)(x-7) = x^2 - 3x + 2 - 7$

$$\begin{array}{r} \underline{x^3 + 2x^2 - 5x + 1} \\ x+3 \end{array}$$

$$\begin{array}{r} x^2 - x - 2 + \frac{7}{x+3} \\ \hline x+3 \left| \begin{array}{r} x^3 + 2x^2 - 5x + 1 \\ -x^3 - 3x^2 \\ \hline -x^2 - 5x \end{array} \right. \\ \hline \begin{array}{r} +x^2 + 3x \\ \hline -2x + 1 \end{array} \\ \hline \begin{array}{r} +2x + 6 \\ \hline +7 \end{array} \end{array}$$

$$(2x^3 + 13x^2 + 9x - 6) \div (2x+3)$$

divide

$$\begin{array}{r}
 x^2 + 5x - 3 \\
 \hline
 2x+3 \overline{)2x^3 + 13x^2 + 9x - 6} \\
 -2x^3 + 3x^2 \\
 \hline
 10x^2 + 9x \\
 -10x^2 - 15x \\
 \hline
 -6x - 6 \\
 + 6x + 9 \\
 \hline
 3
 \end{array}$$

$$(4x^3 - 6x - 11) \div (2x - 4)$$

$$\begin{array}{r} 2x^2 + 4x + 5 + \frac{9}{2x-4} \\ 2x-4 \overline{)4x^3 + 0x^2 - 6x - 11} \\ - 4x^3 + 8x^2 \\ \hline 8x^2 - 6x \\ - 8x^2 + 16x \\ \hline 10x - 11 \\ - 10x + 20 \\ \hline 9 \end{array}$$

divide

$$(x^3 - 64) \div (x - 4)$$
$$\begin{array}{r} x^2 + 4x + 16 \\ \hline x - 4 \overline{)x^3 + 0x^2 + 0x - 64} \\ -x^3 + 4x^2 \\ \hline 4x^2 + 0x \\ -4x^2 + 16x \\ \hline 16x - 64 \\ -16x + 64 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 4x^4 + 3x^3 + 4x^2 + 9x - 6 \\ \hline x + 3 \end{array} \quad \text{divid}$$

$$\begin{array}{r} x^2 + 0x + 3 \overline{)4x^4 + 3x^3 + 4x^2 + 9x - 6} & 4x^2 + 3x - 8 + \frac{18}{x^2 + 3} \\ - 4x^4 - 0x^3 - 12x^2 \\ \hline 3x^3 - 8x^2 + 9x \\ - 3x^3 - 0x^2 - 9x \\ \hline - 8x^2 + 0x - 6 \\ + 8x^2 + 0x + 24 \\ \hline 18 \end{array}$$